MATHEMATICS 1 - MAKEUP 1.1

NAME:

DATE:

Teacher:

Total credit:

Give reasons for all the answers!

1. Find the domain of the function $f(x) = \ln \frac{2-x}{1+x^2}$.

Eval:

2. Differentiate the function $f(x) = (5 + x^2) \sin 5x$.

Eval:

- **3.** Given function $f(x) = 2x^2 5x 3$ and point A = [2, -5]. Is the straight line x + 3y + 13 = 0 tangent line or normal line or nothing to f at the point A?
- **4.** The function $f(x) = \frac{2-\ln x}{x}$ assumes at x = e a local extreme. Yes or not?
- **5.** Decide, if the set of vectors $\vec{u} = (3, -1, 2, 1)$, $\vec{v} = (0, 0, 0, 2)$, $\vec{w} = (6, -2, 4, 2)$ is linearly dependent or independent. **Eval:**
- **6.** Find the rank of the matrix

$$A = \left(\begin{array}{ccc} 3 & 2 & 1 \\ 0 & 0 & 2 \\ 0 & 0 & 7 \end{array}\right).$$

Eval:

7. For $x \in \mathbb{R}$ solve the equation

$$\left| \begin{array}{cc} 4-x & 2\\ 3 & 4-x \end{array} \right| = -6.$$

Eval:

8. Solve the system of linear equations in dependence on $\alpha \in \mathbb{R}$, for which the augmented matrix is as follows

$$\left(\begin{array}{ccc|c} 0 & 1 & | & \alpha \\ 1 & 1 & | & 2 \end{array}\right)$$

Eval:

- **9.** Write the general equation of the line p which passes through the point A = [5, -7] and has the normal vector $\mathbf{n} = (1, -1)$. **Eval:**
- **10.** Find the intersection of the line p: x=1+3t, y=2t, z=3 and the plane $\rho: 2x-y-3z-1=0$. **Eval:**